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Effective computer analysis of event-continuous and hybrid systems is addressed. A multipurpose software architecture employing control of the integration step size with regard to the error, stability, and unilateral events is proposed. The problem of synchronization of continuous and discrete processes is dealt with. All new theoretical concepts are tested on heterogeneous applications to biological systems, large electric power systems, mechanical engineering and chemical kinetics problems.

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