

MINISTRY OF SCIENCE AND HIGHER EDUCATION
OF THE RUSSIAN FEDERATION

SOUTHERN FEDERAL UNIVERSITY

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ANALYTIC GEOMETRY

Textbook

Rostov-on-Don – Taganrog
Southern Federal University Press
2020

UDC 514.122+514.123(075.8)

BBC 22.151.5

P32

*Published by decision of the educational-methodical commission
of the I. I. Vorovich Institute of Mathematics, Mechanics, and Computer Science
of the Southern Federal University (minutes No. 9 dated September 8, 2020)*

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Pilidi, V. S.

P32 Analytic geometry : textbook / V.S. Pilidi ; Southern Federal University.
– Rostov-on-Don ; Taganrog : Southern Federal University Press, 2020. –
195 p.

ISBN 978-5-9275-3576-7

The book contains material on analytic geometry included in the university discipline "Algebra and Geometry". In addition to detailed presentation of theoretical material, there are given problems in the volume that is quite sufficient both for practical classes and for students' independent work. Most problems are provided with detailed solutions. The book is addressed to students of the educational program "Theoretical Computer Science and Information Technologies" and can also be used by students of other educational programs.

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BBC 22.151.5

ISBN 978-5-9275-3576-7

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